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1 Multivariate Data

There are lots of things we could mean by presenting multivariate data.

- Presenting the underlying structure in multivariate data (e.g., biplots).
- Interactive, high-dimensional visualization of the data themselves (e.g., GGobi, Linking and Brushing)
- Interactive 3-d visualization (with rgl or similar).
- Trellis graphs for 2-d representations of multivariate data.

We obviously will not have time to talk about all of these things, given that we have 90 minutes of lecture, but recognize that these are out there and we can talk about anything you want outside of class. Since the course is about presenting statistical results, it is the last of these definitions of “multivariate data” which we will find most useful. These will allow us to make the most of the time we have together and will permit the widest possible range of possibilities in presenting multivariate data.

2 Lattice Graphics

While you can certainly make lattice graphs for the same types of data that we made traditional graphics, the real strength of lattice graphs is with dependent data (i.e., data organized by group). Examples of this would be time-series cross-sectional data (e.g., countries/states/individuals over time) or hierarchically structured data (e.g., students within classrooms within schools). Lattice graphs perform a type of repeated calculation - they make the same plot for each group and present them all in a very nice-looking display.

The work-horse for lattice graphs is the command `xyplot`. This is the lattice analog to the `plot` command in the traditional graphics environment. To make the commands available, you first have to load the lattice package:

```r
> library(lattice)
```

Now, let’s just make a scatterplot of income and prestige from the Duncan data.

```r
> library(car)
> data(Duncan)
> xyplot(prestige ~ income, data=Duncan)
```
This plot looks very similar, but it has a couple of different defaults from the \texttt{plot} command. Specifically, the default color for the plotting symbols is a shade of blue and there are tick marks on each axis, though they’re only labeled on the bottom and left axes. Many of the same parameters work here, so we can change the plotting symbol and color if we want with \texttt{pch} and \texttt{col}.

\begin{verbatim}
> xyplot(prestige ~ income, data=Duncan, pch=16, col="black")
\end{verbatim}

### 2.1 Plotting by groups

There are two different options for plotting by groups with \texttt{lattice}. Superposition is when all group data are plotted in the same region, but groups are distinguished by...
colors, plotting symbols, etc... This is basically what we did with the traditional graphs the other day. Superposition happens by specifying the groups argument. Juxtaposition is when different groups are plotted in different plotting regions (though all within the same larger window). Juxtaposition happens by providing a conditioning statement (e.g., $y \sim x \mid z$ where $z$ is the conditioning variable that will be used to determine what small windows will exist. Now, let’s consider generating this plot, but by the groups defined by occupation type:

```
> xyplot(prestige ~ income | type, data=Duncan, 
  + pch=1, col="black")
```

```
> xyplot(prestige ~ income, data=Duncan, 
  + groups=Duncan$type, 
  + auto.key=list(text=c("Blue Collar", "Professional", "White Collar")))
```

Notice that the only difference here is the $|$ (the pipe character) separating income from the grouping variable type. I also changed the plotting symbol back to an open circle. When a grouping variable is used, R makes the first plot in the lower left-hand corner and then fills in the rows of the plotting region until it’s done. If you want to change this behavior (so it fills in the upper left-hand cell first), you can issue the argument as.table=T.

```
> xyplot(prestige ~ income | type, data=Duncan, pch=1, col="black", 
  + as.table=T)
```
Now, let’s try to remake the same graph that we made before - with different plotting symbols based on type. We could make the original plot (without lines or a legend as follows):

```r
> trellis.par.set(superpose.line=list(col=c("blue", "black", "red")), 
+   superpose.symbol = list(col=c("blue", "black", "red"), pch=1:3)) 
> xyplot(prestige ~ income, data=Duncan, groups=Duncan$type, 
+   auto.key=list(text=c("Blue Collar", "Professional", "White Collar")))
```

Remember, that one way we could do this with `plot` was to create a vector of plotting symbols - one for each observation. Here, we’re using lattice’s built-in superposition function and telling R that we want the three groups to have plotting symbols of 1, 2, and 3, and colors blue, black and red. Adding the lines gets more complicated. The complication here comes from the fact that in lattice graphs, you must do everything at once (sort of). To do this, you have to define a function (hence the reason the function-writing day came before the lattice day).

Here, we need to specify the panel function argument to `xyplot`. The panel function is a function of the `x` and `y` arguments to the `xyplot` command. In the panel function, you can use the following analogs to the pieces in the traditional graphics sytem.

- `panel.lines(...)`
- `panel.points(...)`
- `panel.segments(...)`
- `panel.text(...)`
- `panel.rect(...)`
- `panel.arrows(...)`
- `panel.polygon(...)`

These generally work in a similar fashion to their traditional graphics counterparts. The `panel.superpose` function is how you can use the functions above in conjunction with the `groups` argument to `xyplot()`. We could remake the graph above by specifying the following panel function:
> trellis.par.set(superpose.line=list(col=c("blue", "black", "red")),
+        superpose.symbol = list(col=c("blue", "black", "red"), pch=1:3))
> xyplot(prestige ~ income, data=Duncan, groups=Duncan$type,
+        auto.key=list(text=c("Blue Collar", "Professional", "White Collar")),
+        panel = function(...){
+            panel.superpose(..., panel.groups="panel.xyplot")
+            panel.superpose(..., panel.groups="panel.lmline")
+        })
2.1.1 Adding Two Plots Together

If we wanted to restrict ourselves to the observed ranges of x by subgroup, we could do:

```r
> panel.lmseg <- function(x,y,...){
+   tmp.mod <- lm(as.numeric(y) ~ as.numeric(x))
+   tmp.pred <- fitted(tmp.mod)
+   ord.x <- order(x)
+   tmp.x <- x[ord.x]
+   tmp.y <- tmp.pred[ord.x]
+   panel.lines(tmp.x, tmp.y,...)
+ }
> trellis.par.set(superpose.line=list(col=c("blue", "black", "red")),
+   superpose.symbol = list(col=c("blue", "black", "red"), pch=1:3))
> xy1 <- xyplot(prestige ~ income, data=Duncan, groups=Duncan$type,
+   auto.key=list(text=c("Blue Collar", "Professional", "White Collar")))
> xy2 <- xyplot(prestige ~ income, data=Duncan, groups=Duncan$type, type="l",
+   panel = function(x,y,...){
+     panel.superpose(x,y, panel.groups="panel.lmseg",...)
+   }
+ }
> library(latticeExtra)
> xy1 + xy2
```

![Graph showing income vs. prestige for different subgroups](image)
2.2 More on Juxtaposed Plots

Since Lattice’s biggest benefit is the juxtaposed panels, we can investigate these solutions a bit starting with our initial juxtaposed plot from before.

```r
> xyplot(prestige ~ income | type, data=Duncan,
+     pch=1, col="black",
+     panel = function(x,y,subscripts,...){
+         panel.points(x,y,...)
+     })
```
We could add a regression line in each panel by adding something to the panel function.

```r
> old.levs <- levels(Duncan$type)
> levels(Duncan$type) <- c("Blue Collar", "Professional", "White Collar")
> xyplot(prestige ~ income | type, data=Duncan,
+     pch=1, col="black", layout=c(3,1),
+     aspect=1, panel = function(x,y,subscripts,...){
+       panel.points(x,y,...)
+       panel.lmline(x,y,...)
+     })
> levels(Duncan$type) <- old.levs
```

We can also exert some finer control over multi-panel displays. This is where things get a little weird, though. The panel function tells R what to do in each panel for the variables x and y by groups. So, let’s go back to the argument above. The `panel.superpose()` function is a bit difficult to deal with sometimes, but by juxtaposing (rather than superposing) you often don’t have to worry about different plotting characters and the like.
You can add in different data (not either x or y), but you have to specify the subscripts argument to the panel function. Here’s an example of adding in another set of points (prestige vs education) in the same panel for each occupation type.

```r
> xyplot(prestige ~ income | type, data=Duncan, as.table=T,
+     xlim=c(0,100), xlab = "X",
+     panel=function(x,y,subscripts){
+         panel.points(x,y, pch=1, col="black")
+         panel.points(Duncan$education[subscripts], y, col="red", pch=2)
+     }, key=list(space="top", points=list(pch=c(1,2), col=c("black", "red")),
+ text=list(c("Income", "Education"))))
```

Subscripts identify the points in each panel and then allow you to subset other data from the same source (i.e., with the same observations in the rows).
2.3 Example: Plotting Linear Model Results

This example will pull together a lot of pieces that we’ve worked with already. First, let’s figure out the steps that we want to go through.

1. Run model(s) - here we’ll use 2 models.
2. Generate predictions changing one variable and holding all other variables constant.
3. Manipulate data to produce a data frame that can be plotted.
4. Make the plot.

2.3.1 Run the Model(s)

Here, we’ll estimate a model that is linear in income and one that has a polynomial fit in income from the Duncan data.

> mod1 <- lm(prestige ~ income + education + type, data=Duncan)
> mod2 <- lm(prestige ~ poly(income, 3) + education + type, data=Duncan)

2.3.2 Generate Predictions

Now, we have to generate predictions based

> newdat <- data.frame(
+ income = seq(min(Duncan$income), max(Duncan$income), length=25),
+ education = mean(Duncan$education),
+ type = "bc"
+ )
> p1 <- as.data.frame(predict(mod1, newdata=newdat, interval="confidence"))
> p2 <- as.data.frame(predict(mod2, newdata=newdat, interval="confidence"))

2.3.3 Manipulate Data

Now, we have to take the two sets of predictions and make a single data frame.

> plot.dat <- as.data.frame(rbind(p1, p2))

Next, we need to identify which predictions are from which model. The first 25 are from model 1 and the second 25 are from model 2. We also need to add in the income variable for plotting.

> plot.dat$model <- rep(c("Model 1", "Model 2"), each=25)
> plot.dat$income <- rep(newdat$income, 2)
> rownames(plot.dat) <- NULL
2.3.4 Make the Plot

We can make the plot using a panel function that incorporates the lower and upper bounds with different line-types.

```r
> xyplot(fit ~ income | model, data=plot.dat,
+       aspect=1,
+       xlab = "Income", ylab = "Predicted Prestige",
+       lower = plot.dat$lwr, upper = plot.dat$upr,
+       panel = function(x,y,subscripts, lower, upper){
+         panel.lines(x,y, col="black")
+         panel.lines(x, lower[subscripts], lty=2, col="black")
+         panel.lines(x, upper[subscripts], lty=2, col="black")
+     })
```
I’ve written a panel function and a `prepanel` function (which basically finds the right axis limits) and they are both in the `DAMisc` package.

```r
> library(DAMisc)
> xyplot(fit ~ income | model, data=plot.dat,
+     aspect = 1,
+     xlab = "Income", ylab = "Predicted Prestige",
+     lower=plot.dat$lwr,upper=plot.dat$upr,
+     panel = panel.ci, zl=F, prepanel=prepanel.ci)
```

![Plot of predicted prestige vs income for two models](image)
You could put them in the same plotting region with semi-transparent confidence bounds with the following. Here, the `groups` argument works sort of like `subscripts`, but not exactly:

```r
#panel.transci <- function(x,y,groups,lower,upper,...){
#    panel.polygon(
#        x=c(x[groups == "Model 1"], rev(x[groups == "Model 1"])),
#        y = c(lower[groups == "Model 1"], rev(upper[groups == "Model 1"])),
#        col = rgb(1,0,0,.25,1), border="transparent")
#    panel.polygon(
#        x=c(x[groups == "Model 2"], rev(x[groups == "Model 2"])),
#        y = c(lower[groups == "Model 2"], rev(upper[groups == "Model 2"])),
#        col = rgb(0,0,1,.25,1), border="transparent")
#    panel.lines(x[groups == "Model 1"], y[groups == "Model 1"], col="red", lwd=1.5)
#    panel.lines(x[groups == "Model 2"], y[groups == "Model 2"], col="blue", lwd=1.5)
#}
#trellis.par.set(
#    superpose.line = list(col=c("red", "blue")),
#    superpose.polygon = list(col=c(rgb(1,0,0,.25,1), rgb(0,0,1,.25,1))))
#xyplot(fit ~ income, groups=model, data=plot.dat,
#    xlab = "Income", ylab = "Predicted Prestige",
#    lower=plot.dat$lwr,upper=plot.dat$upr,
#    panel = panel.transci, prepanel=prepanel.ci,
#    key = list(space="top",
#        points=list(pch=15, col=c(rgb(1,0,0,.25,1), rgb(0,0,1,.25,1)), cex=1.5),
#        text=list(c("Model 1", "Model 2")),
#        lines=list(lty=c(1,1), lwd=c(1.5,1.5), col=c("red", "blue")))
```

![Graph showing predicted prestige vs income for two models with semi-transparent confidence bounds for each model.](image_url)
2.4 Other Lattice Graphs

Lattice has some other options, too. These are generally wrappers to \texttt{xyplot}, but they have different default behavior for different situations.

2.4.1 Histograms

The \texttt{histogram} function makes histograms in the lattice package. The \texttt{hist()} command is the traditional graphics analog. In \texttt{hist}, the option \texttt{freq} can either be true (T) indicating you want counts or false (F) meaning you want density on the y-axis. In \texttt{histogram()}, the argument \texttt{type} can equal 'count', 'percent' or 'density'.

\begin{verbatim}
> histogram(~prestige, data=Duncan, nint=10, type="count",
          + endpoints=c(0,100), col="transparent")
\end{verbatim}
2.4.2 Density Plots

We could also make density plots in a similar fashion using `plot` and the function `density` or using `densityplot` from lattice.

```r
> densityplot(~income, data=Duncan,
+   col = "black", plot.points=F)
```

![Density Plot](image-url)
The two (densities and histograms) can be combined as follows:

```r
> xyplot(~prestige, data=Duncan,
+     ylim=c(0,.02), xlim=c(-5,105),
+     panel = function(x){
+       panel.histogram(x,
+         breaks=seq(0,100,10),
+         col="gray80",
+         endpoints=c(0,100))
+       panel.densityplot(x,
+         darg=list(n=100),
+         col="red",
+         lwd=1.5,
+         plot.points=F)
+     })
```

You could also do the same thing, but by juxtaposing on some other variable (e.g., country). Here is a histogram of assets from the Ornstein data, separated by nation.

```r
> data(Ornstein)
> b <- with(Ornstein, do.breaks(range(log2(assets)), 10))
> xyplot(~log2(assets) | nation, data=Ornstein,
+       xlim = range(b), ylim=c(0,.3),
+       panel = function(x){
+         panel.histogram(x,
+         breaks=b,
+         col="gray80",
+         #endpoints=c(0,100)
+         )
+       panel.densityplot(x,
+         darg=list(n=100),
+         col="red",
+         lwd=1.5,
+         plot.points=F)
+ })
```

![Histogram of assets separated by nation](image)
2.4.3 Bar plot

Just as before (with the traditional graphs), you need to aggregate to get mean values (or some other statistic that will provide the height for the bar plot). Here, we could aggregate over just one value as above.

> data(Chile)
> ag <- with(Chile, aggregate(income,
+   list(region), mean, na.rm=T))
> ag <- ag[-1]
> names(ag) <- levels(Chile$region)
> barplot(ag)
You could also do side-by-side barplots by aggregating over two variables.

```r
> ag <- with(Chile, aggregate(income,
+    list(region, education), mean, na.rm=T))
> agmat <- matrix(ag[,3], ncol=3, nrow=5)
> colnames(agmat) <- levels(Chile$education)
> rownames(agmat) <- levels(Chile$region)
> barplot(agmat, beside=T, legend.text=T)
```
2.4.4 Dotplots

> library(gmodels)
> ag1 <- with(Chile, by(income, list(region), ci, na.rm=T))
> ag1 <- do.call(rbind, ag1)
> colnames(ag1) <- c("mean", "lower", "upper", "se")
> ag1 <- as.data.frame(ag1)
> ag1 <- ag1[order(ag1$mean), ]
> ag1$region <- factor(1:nrow(ag1),
+  levels=1:nrow(ag1), labels=rownames(ag1))
> dotplot(region ~ mean, data=ag1, xlab="income")
You could “roll your own” dotplot by using `xyplot`.

```r
> xyplot(region ~ mean, data=ag1,
+       lower=ag1$lower, upper=ag1$upper,
+       panel = function(x,y,lower,upper,...){
+           panel.segments(lower, y, upper, y, col="black")
+           panel.points(x,y, pch=16, col="black")
+       }, xlim=c(20000, 46000))
```

![Dotplot diagram](image-url)
You could also do this by groups as follows:

```r
> ag2 <- with(Chile, aggregate(income,
+     list(region, education), ci, na.rm=T))
> ag2 <- cbind(ag2[,1:2], ag2$x)
> names(ag2) <- c("region", "education", "mean", "lower", "upper", "se")
> ag2 <- ag2[order(ag2$education, ag2$mean), ]
> ag2$region <- factor(ag2$region,
+     levels=ag2$region[which(ag2$education == "PS")])
> xyplot(region ~ mean | education, data=ag2,
+     lower=ag2$lower, upper=ag2$upper,
+     panel = function(x,y,subscripts,lower,upper,...){
+         panel.segments(lower[subscripts], y,
+         upper[subscripts], y, col="black")
+         panel.points(x,y, pch=16, col="black")
+     },
+     xlim=c(13000, 101500),
+     layout = c(1,3), as.table=T)
```
2.5 A closer look at superposed series

Different series can be distinguished in superposed plots by using the `groups` argument in a lattice plot. This is relatively straightforward for simple plots, but customization here is a bit more challenging. Imagine that we wanted to mimic something that Cleveland suggested earlier in our discussion?
Doing either the top 3 plots or the bottom single plot is easy.

```r
> set.seed(1234)
> x <- 1:20
> y1 <- sort(rnorm(20))
> y2 <- sort(rnorm(20))
> y3 <- sort(rnorm(20))
> half <- runif(20, .25,.75)
> l1 <- y1-half
> l2 <- y2-half
> l3 <- y3-half
> u1 <- y1+half
> u2 <- y2+half
> u3 <- y3+half
> mydata <- data.frame(x, y1,y2,y3,
+ l1,l2,l3, u1,u2,u3)
> head(mydata)
   x  y1  y2  y3  l1  l2  l3  u1  u2  u3
1  1 -2.35 -2.2 -2.1 -2.9 -2.8 -2.4 -1.7
2  2 -1.21 -1.6 -1.3 -1.9 -2.3 -1.9 -0.5
3  3 -1.00 -1.4 -1.2 -1.7 -2.2 -1.9 -0.3
4  4 -0.91 -1.4 -1.1 -1.7 -2.1 -1.8 -0.2
5  5 -0.89 -1.7 -1.7 -1.8 -2.2 -1.8 -0.4
6  6 -0.84 -1.2 -1.1 -1.6 -2.1 -1.4 -0.4
> df <- data.frame(x=x, y = c(y1, y2, y3),
+ lower = c(l1, l2, l3),
+ upper = c(u1, u2, u3))
> df$group <- factor(rep(c("Group 1", "Group 2", "Group 3"), each=20))
> xyplot(y ~ x | group, data=df, lower=df$lower, upper=df$upper,
+ zl=F, layout = c(1,3),
+ prepanel=prepanel.ci, panel = panel.ci)
```

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Putting them together is a bit more challenging. Using the "+" operator from the latticeExtra package won't work. First, let's consider what the data will look like:
The u variables are upper confidence bounds and the l variables are lower confidence bounds. You could have these or not depending on your application. Otherwise, you could have a set of standard deviation variables that will be reshaped to long and you could make variables lower and upper from the y and sd variables.
We can use a function in today's code file called makelong to make data that is amenable to plotting this way:

```r
> longdata <- makelong(mydata, x="x", yvars=c("y1", "y2", "y3"),
+                      lowers=c("l1", "l2", "l3"), uppers=c("u1", "u2", "u3"))
```

You could include a grouplabs argument that will allow you to label the groups. It can have either A) as many names as there are y variables in your original data (in which case the panel for all lines will be labeled “All”) or B) as many names as there are y variables plus one for the panel with all lines. Next, we can set the colors for the lines. The first one should be 'black', but the others can be whatever you like. Since we have three groups, we need to have a sequence of colors that is 'black' plus three other colors.

```r
> library(RColorBrewer)
> cols <- brewer.pal(3, "Dark2")
> trellis.par.set(superspose.line=list(col=c("black", cols)))
```

Then, we can set the range of the y-axis

```r
> range(c(longdata[,c("lower", "upper")]), na.rm=T)
[1] -2.967836  3.100414
```

```r
> y1 <- c(-3.25, 3.25)
```
Finally, we could use the following plotting function:

```r
> levs <- levels(longdata$group)
> levs <- levs[-length(levs)]
> xyplot(y ~ x| group, data=longdata, group=g2, type="l", as.table=T, ylab=yl,
+     lower = longdata$lower, upper=longdata$upper, zl=FALSE, layout = c(1,4),
+     panel = function(x,y,groups,subscripts, lower=lower, upper=upper,...){
+     panel.superpose(x,y,groups=groups, subscripts=subscripts,..., panel.groups=panel.xyplot)
+     panel.superpose(x=c(x, rev(x), x[1]),
+             y=c(lower[subscripts], rev(upper[subscripts]), lower[subscripts][1]),
+            groups=groups, subscripts=subscripts, ..., panel.groups=panel.polygon,
+            col=rgb(.75,.75,.75,.25), border=NA)
+     },
+     key = list(space="top", columns=2, lines=list(col=cols, lty=1), text=list(levs)))
```

![Plot](image)

---

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